

**KLA Year 10 FOUNDATION  
Term 1 Maths Knowledge  
Organisers**



# Year 10 – Foundation Knowledge Organiser Half Term 1

## Key Topics and Vocabulary

### Standard Form

Standard Form

Multiplying or Dividing with Standard Form

Adding or Subtracting with Standard Form

### Pythagoras' theorem

Pythagoras' Theorem

### Trigonometry

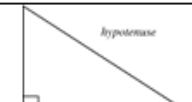
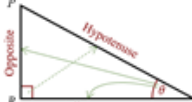



Exact Values for Angles in Trigonometry

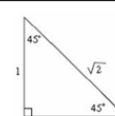
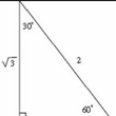
Trigonometry

Hypotenuse

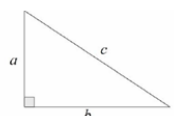
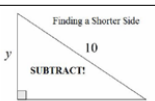
Adjacent

Trigonometric Formulae

Topic/Skill	Definition/Tips	Example
1. Trigonometry	The study of triangles.	
2. Hypotenuse	The longest side of a right-angled triangle. Is always opposite the right angle.	
3. Adjacent	Next to	
4. Trigonometric Formulae	Use SOHCAHTOA. $\sin \theta = \frac{O}{H}$ $\cos \theta = \frac{A}{H}$ $\tan \theta = \frac{O}{A}$  When finding a missing angle, use the 'inverse' trigonometric function by pressing the 'shift' button on the calculator.	 Use 'Opposite' and 'Adjacent', so use 'tan' $\tan 35 = \frac{x}{11}$ $x = 11 \tan 35 = 7.70 \text{ cm}$  Use 'Adjacent' and 'Hypotenuse', so use 'cos' $\cos x = \frac{5}{7}$ $x = \cos^{-1}\left(\frac{5}{7}\right) = 44.4^\circ$

Topic/Skill	Definition/Tips	Example																								
1. Exact Values for Angles in Trigonometry	<table border="1"> <thead> <tr> <th></th> <th>0°</th> <th>30°</th> <th>45°</th> <th>60°</th> <th>90°</th> </tr> </thead> <tbody> <tr> <td>sin</td> <td>0</td> <td><math>\frac{1}{2}</math></td> <td><math>\frac{\sqrt{2}}{2}</math></td> <td><math>\frac{\sqrt{3}}{2}</math></td> <td>1</td> </tr> <tr> <td>cos</td> <td>1</td> <td><math>\frac{\sqrt{3}}{2}</math></td> <td><math>\frac{\sqrt{2}}{2}</math></td> <td><math>\frac{1}{2}</math></td> <td>0</td> </tr> <tr> <td>tan</td> <td>0</td> <td><math>\frac{1}{\sqrt{3}}</math></td> <td>1</td> <td><math>\sqrt{3}</math></td> <td>---</td> </tr> </tbody> </table>		0°	30°	45°	60°	90°	sin	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	cos	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	tan	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	---	 
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Topic/Skill	Definition/Tips	Example
1. Standard Form	$A \times 10^b$ where $1 \leq A < 10$ , $b = \text{integer}$	$8400 = 8.4 \times 10^3$ $0.00036 = 3.6 \times 10^{-4}$
2. Multiplying or Dividing with Standard Form	Multiply: <b>Multiply the numbers and add the powers.</b> Divide: <b>Divide the numbers and subtract the powers.</b>	$(1.2 \times 10^3) \times (4 \times 10^6) = 8.8 \times 10^9$ $(4.5 \times 10^5) \div (3 \times 10^2) = 1.5 \times 10^3$
3. Adding or Subtracting with Standard Form	Convert in to ordinary numbers, calculate and then convert back in to standard form	$2.7 \times 10^4 + 4.6 \times 10^3$ $= 27000 + 4600 = 31600$ $= 3.16 \times 10^4$

Topic/Skill	Definition/Tips	Example
1. Pythagoras' Theorem	For any right angled triangle: $a^2 + b^2 = c^2$ 	<p>Finding a Shorter Side</p>  SUBTRACT: $a = y, b = 8, c = 10$ $a^2 = c^2 - b^2$ $y^2 = 100 - 64$ $y^2 = 36$ $y = 6$
	Used to find <b>missing lengths</b> . a and b are the shorter sides, c is the <b>hypotenuse (longest side)</b> .	

# Year 10 – Foundation Knowledge Organiser Half Term 2

## Key Vocabulary

### Algebra quadratics, rearranging formulae and identities

#### Quadratic

#### Factorising Quadratics

#### Difference of Two Squares

Solving Quadratics ( $ax^2 = b$ )

Solving Quadratics ( $ax^2 + bx = 0$ )

#### Solving Quadratics by Factorising

( $a = 1$ )

Factorising Quadratics when  $a \neq 1$

#### Solving Quadratics by Factorising

( $a \neq 1$ )

### Collecting and Representing Data

Frequency Table

Bar Chart

Types of Bar Chart

Pie Chart

Pictogram

Line Graph

Two Way Tables

Topic/Skill	Definition/Tips	Example																					
1. Frequency Table	A record of <b>how often each value</b> in a set of data occurs.	<table border="1"> <thead> <tr> <th>Number of marks</th> <th>Tally marks</th> <th>Frequency</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>    </td> <td>4</td> </tr> <tr> <td>2</td> <td>    </td> <td>4</td> </tr> <tr> <td>3</td> <td>    </td> <td>4</td> </tr> <tr> <td>4</td> <td>    </td> <td>4</td> </tr> <tr> <td>5</td> <td>    </td> <td>4</td> </tr> <tr> <td>Total</td> <td></td> <td>16</td> </tr> </tbody> </table>	Number of marks	Tally marks	Frequency	1		4	2		4	3		4	4		4	5		4	Total		16
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2. Bar Chart	Represents data as vertical blocks.  $x$ - axis shows the <b>type of data</b> $y$ - axis shows the <b>frequency</b> for each type of data Each bar should be the <b>same width</b> There should be <b>gaps</b> between each bar Remember to <b>label</b> each axis.																						
3. Types of Bar Chart	<b>Compound/Composite Bar Charts</b> show data stacked on top of each other.  <b>Comparative/Dual Bar Charts</b> show data side by side.																						
4. Pie Chart	Used for showing <b>how data breaks down into its constituent parts</b> .  When drawing a pie chart, <b>divide 360° by the total frequency</b> . This will tell you how many degrees to use for the frequency of each category.  Remember to <b>label</b> the category that each sector in the pie chart represents.	<p>If there are 40 people in a survey, then each person will be worth <math>360 \div 40 = 9^\circ</math> of the pie chart.</p>																					

5. Pictogram	Uses <b>pictures</b> or symbols to <b>show the value</b> of the data.  A pictogram must have a <b>key</b> .	<p>Black    </p> <p>Red    </p> <p>Green </p> <p>Others    </p> <p> = 4 cars</p>																																																
6. Line Graph	A graph that uses <b>points connected by straight lines</b> to show how data changes in values.  This can be used for <b>time series data</b> , which is a series of data points spaced over uniform time intervals in <b>time order</b> .																																																	
7. Two Way Tables	A table that <b>organises data around two categories</b> .  Fill out the information step by step using the information given.  Make sure all the totals add up for all columns and rows.	<p>Question: Complete the 2 way table below.</p> <table border="1"> <thead> <tr> <th></th> <th>Left Handed</th> <th>Right Handed</th> <th>Total</th> </tr> </thead> <tbody> <tr> <td>Boys</td> <td>10</td> <td></td> <td>58</td> </tr> <tr> <td>Girls</td> <td></td> <td></td> <td>42</td> </tr> <tr> <td>Total</td> <td>10</td> <td></td> <td>100</td> </tr> </tbody> </table> <p>Answer: Step 1, fill out the easy parts (the totals)</p> <table border="1"> <thead> <tr> <th></th> <th>Left Handed</th> <th>Right Handed</th> <th>Total</th> </tr> </thead> <tbody> <tr> <td>Boys</td> <td>10</td> <td>48</td> <td>58</td> </tr> <tr> <td>Girls</td> <td>0</td> <td>42</td> <td>42</td> </tr> <tr> <td>Total</td> <td>10</td> <td>90</td> <td>100</td> </tr> </tbody> </table> <p>Answer: Step 2, fill out the remaining parts</p> <table border="1"> <thead> <tr> <th></th> <th>Left Handed</th> <th>Right Handed</th> <th>Total</th> </tr> </thead> <tbody> <tr> <td>Boys</td> <td>10</td> <td>48</td> <td>58</td> </tr> <tr> <td>Girls</td> <td>0</td> <td>42</td> <td>42</td> </tr> <tr> <td>Total</td> <td>10</td> <td>90</td> <td>100</td> </tr> </tbody> </table>		Left Handed	Right Handed	Total	Boys	10		58	Girls			42	Total	10		100		Left Handed	Right Handed	Total	Boys	10	48	58	Girls	0	42	42	Total	10	90	100		Left Handed	Right Handed	Total	Boys	10	48	58	Girls	0	42	42	Total	10	90	100
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Topic/Skill	Definition/Tips	Example
1. Quadratic	A quadratic expression is of the form  $ax^2 + bx + c$  where $a$ , $b$ and $c$ are numbers, $a \neq 0$	Examples of quadratic expressions: $x^2$ $8x^2 - 3x + 7$  Examples of non-quadratic expressions: $2x^3 - 5x^2$ $9x - 1$
2. Factorising Quadratics	When a quadratic expression is in the form $x^2 + bx + c$ find the two numbers that <b>add to give <math>b</math> and multiply to give <math>c</math></b> .	$x^2 + 7x + 10 = (x + 5)(x + 2)$ (because 5 and 2 add to give 7 and multiply to give 10)  $x^2 + 2x - 8 = (x + 4)(x - 2)$ (because +4 and -2 add to give +2 and multiply to give -8)
3. Difference of Two Squares	An expression of the form $a^2 - b^2$ can be factorised to give $(a + b)(a - b)$	$x^2 - 25 = (x + 5)(x - 5)$ $16x^2 - 81 = (4x + 9)(4x - 9)$
4. Solving Quadratics ( $ax^2 = b$ )	Isolate the $x^2$ term and square root both sides. Remember there will be a <b>positive and a negative solution</b> .	$2x^2 = 98$ $x^2 = 49$ $x = \pm 7$
5. Solving Quadratics ( $ax^2 + bx = 0$ )	<b>Factorise</b> and then solve = 0.	$x^2 - 3x = 0$ $x(x - 3) = 0$ $x = 0$ or $x = 3$

## Knowledge Questions

Below are a series of questions.

Use these to apply your knowledge and practice.

## Circumference and area

Is the diameter of a circle also a chord? Why or why not?  
What's the difference between a segment and a sector?

## Basic trigonometry

Will the ratio remain constant if the given angle gets bigger/smaller? Why/Why not?

## Basic Algebra

What does the word solve mean? What connection does this have to the word solution?

## Algebra quadratics, rearranging formula and identities

Which letter is the subject of the formula? How do you know?

## Collecting and representing data

Why do statisticians take samples rather than interview the whole population?

## Knowledge Checklist

KNOWLEDGE  
PROGRESS

KNOWLEDGE CHECKLIST		R	A	G
1	Circumference and area			
2	Basic trigonometry			
3	Basic algebra			
4	Algebra quadratics, rearranging formula and identities			
5	Collecting and representing data			
6				
7				
8				
9				
10				

## High Flyers - Enrichment Task



Use the information on the first triangle to find the missing values  $x$  on the following two triangles.

